

If we do not care about the ordering of the choices, only the elements, we can define **combinations** as $\binom{n}{k}$, which is read “ n choose k ”.

$$\binom{n}{k} = \frac{n!}{(n-k)!k!}$$

$\binom{n}{k}$ is also equal to the $k + 1$ th number on the $n + 1$ th row of Pascal’s Triangle.

Using combinations, we now have a tool to calculate the probability that an event with probability p will occur exactly k times in an experiment repeated n times.

$$\binom{n}{k} p^k (1-p)^{n-k}$$

And therefore assuming n is odd, the probability that the majority is correct when each individual is correct with probability p is

$$\sum_{k=\lceil \frac{n}{2} \rceil}^n \binom{n}{k} p^k (1-p)^{n-k}$$